

# Prime Numbers



**Count Von Count explains that 24 has 8 factors**  
**{Factors of 24} = {1, 2, 3, 4, 6, 8, 12, 24}**  
**He asks, “Is 24 a prime number ?”**

## 5.1 How many factors ?

In the lesson on *Factor Rainbows* we saw that 144 has the factors,

$$\{\text{Factors of 144}\} = \{1, 2, 3, 4, 6, 8, 9, 12, 16, 18, 24, 36, 48, 72, 144\}$$

The curly brackets indicate that this is a *set*; a collection of numbers.

We can count how many factors are in this set.

$$n\{\text{Factors of 144}\} = 15$$

Notice the  $n$  stands for “number of”.

## 5.2 Exercise

Marks available : 30

### Question 1

What is  $n\{\text{Factors of 6}\}$  ?

[ 2 marks]

### Question 2

What is  $n\{\text{Factors of 30}\}$  ?

[ 2 marks ]

### Question 3

The table below lists all of the integers between 1 and 100 (in black), giving each its own square. Also in each square is a smaller number (in red). What is the smaller number telling you about the bigger number ?

[ 2 marks ]

1 <sub>1</sub>	2 <sub>2</sub>	3 <sub>2</sub>	4 <sub>3</sub>	5 <sub>2</sub>	6 <sub>4</sub>	7 <sub>2</sub>	8 <sub>4</sub>	9 <sub>3</sub>	10 <sub>4</sub>
11 <sub>2</sub>	12 <sub>6</sub>	13 <sub>2</sub>	14 <sub>4</sub>	15 <sub>4</sub>	16 <sub>5</sub>	17 <sub>2</sub>	18 <sub>6</sub>	19 <sub>2</sub>	20 <sub>6</sub>
21 <sub>4</sub>	22 <sub>4</sub>	23 <sub>2</sub>	24 <sub>8</sub>	25 <sub>3</sub>	26 <sub>4</sub>	27 <sub>4</sub>	28 <sub>6</sub>	29 <sub>2</sub>	30 <sub>8</sub>
31 <sub>2</sub>	32 <sub>6</sub>	33 <sub>4</sub>	34 <sub>4</sub>	35 <sub>4</sub>	36 <sub>9</sub>	37 <sub>2</sub>	38 <sub>4</sub>	39 <sub>4</sub>	40 <sub>8</sub>
41 <sub>2</sub>	42 <sub>8</sub>	43 <sub>2</sub>	44 <sub>6</sub>	45 <sub>6</sub>	46 <sub>4</sub>	47 <sub>2</sub>	48 <sub>10</sub>	49 <sub>3</sub>	50 <sub>6</sub>
51 <sub>4</sub>	52 <sub>6</sub>	53 <sub>2</sub>	54 <sub>8</sub>	55 <sub>4</sub>	56 <sub>8</sub>	57 <sub>4</sub>	58 <sub>4</sub>	59 <sub>2</sub>	60 <sub>12</sub>
61 <sub>2</sub>	62 <sub>4</sub>	63 <sub>6</sub>	64 <sub>7</sub>	65 <sub>4</sub>	66 <sub>8</sub>	67 <sub>2</sub>	68 <sub>6</sub>	69 <sub>4</sub>	70 <sub>8</sub>
71 <sub>2</sub>	72 <sub>12</sub>	73 <sub>2</sub>	74 <sub>4</sub>	75 <sub>6</sub>	76 <sub>6</sub>	77 <sub>4</sub>	78 <sub>8</sub>	79 <sub>2</sub>	80 <sub>10</sub>
81 <sub>5</sub>	82 <sub>4</sub>	83 <sub>2</sub>	84 <sub>12</sub>	85 <sub>4</sub>	86 <sub>4</sub>	87 <sub>4</sub>	88 <sub>8</sub>	89 <sub>2</sub>	90 <sub>12</sub>
91 <sub>4</sub>	92 <sub>6</sub>	93 <sub>4</sub>	94 <sub>4</sub>	95 <sub>4</sub>	96 <sub>12</sub>	97 <sub>2</sub>	98 <sub>6</sub>	99 <sub>6</sub>	100 <sub>9</sub>

### Question 4

Use the table to write down,

( i )  $n\{\text{Factors of } 93\}$

[ 1 mark ]

( ii )  $n\{\text{Factors of } 52\}$

[ 1 mark ]

( iii )  $n\{\text{Factors of } 66\}$

[ 1 mark ]

( iv )  $n\{\text{Factors of } 97\}$

[ 1 mark ]

### Question 5

It turns out that numbers with exactly 2 factors are of extraordinary importance. So much so that they are given a special name.

They are the *prime* numbers.

( i ) On the table shade out (get rid of) all the numbers that are NOT prime.

[ 6 marks ]

( ii ) How many prime numbers are there less than 100 ?

[ 1 mark ]

( iii ) Explain why 91 is NOT a prime number.

[ 1 mark ]

( iv ) Explain why 89 is a prime number.

[ 1 mark ]

### Question 6

( i ) Draw a factor rainbow for 84

[ 9 marks ]

( ii ) Write in a list, all the factors of 84

[ 1 mark ]

( iii ) Write in a list, all the *prime* factors of 84

[ 1 mark ]

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In October 2020, Shrewsbury School was voted "**Independent School of the Year 2020**"

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Teachers may obtain detailed worked solutions to the exercises by email from [mhh@shrewsbury.org.uk](mailto:mhh@shrewsbury.org.uk)