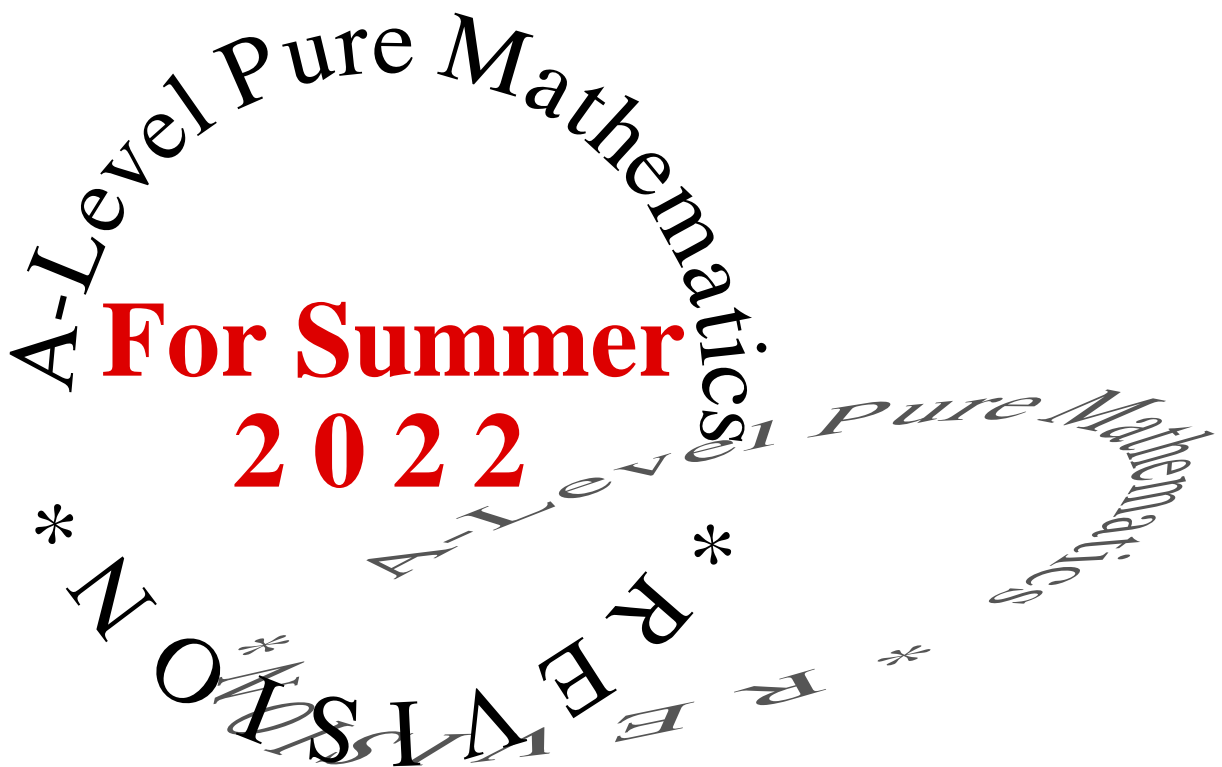


GRADE GRABBER

Numbers 1 to 5

(With answers)



Grade Grabber 1

*Any solution based entirely on graphical
or numerical methods is not acceptable*

Marks Available : 34

Question 1

Given that

$$\sum_{m=1}^k 7m + 3 = 777$$

determine the value of the integer constant k

[4 marks]

Question 2

Sid claims that it's always true that

$$x^2 < (x + 1)^2$$

Exhibit a counter-example that shows Sid's claim is not true

[2 marks]

Question 3

The equation

$$5x^2 + k = 3x + 7$$

has two distinct real roots.

Find the range of possible values for k .

[4 marks]

Question 4

A circle of radius r cm is divided by two radii into two sectors.

The smaller sector has perimeter $(2r + 4)$ cm and the larger sector has area 12 cm^2 .

Calculate the value of r correct to 3 decimal places.

[6 marks]

Question 5

- (i) Use the binomial theorem to write $\frac{1}{(1-x)^3}$ as a polynomial, in ascending powers of x , up to and including the term in x^3

[4 marks]

- (ii) By spotting a connection with the triangular numbers, state the coefficient in the expansion of x^8

[2 marks]

Question 6

Given that

$$f(x) = e^{5x} - 1, \quad x \in \mathbb{R}$$

find $f^{-1}(x)$ and state its domain.

[4 marks]

Question 7

With respect to a fixed origin O , the points A and B have coordinates $(-4, 0)$ and $(12, 12)$ respectively.

The mid-point of AB is M .

Find an equation of the line in the plane of the coordinate axes Ox and Oy which passes through M and is perpendicular to AB .

Hence, or otherwise, find, in cartesian form, an equation of the circle which passes through O , A and B .

[8 marks]

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In October 2020, Shrewsbury School was voted "**Independent School of the Year 2020**"

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Teachers may obtain detailed worked solutions to the exercises by email from mhh@shrewsbury.org.uk