# A-Level Pure Mathematics: Year 1 <br> Progress Test Revision 

### 5.1 Example

The line with equation $y=3 x+1$ is a tangent to a circle with centre ( 30,21 ) (i) Find the equation of the circle.

The line with equation $y=3 x+k, \quad k \neq 1$, is also a tangent to the circle (ii) Find the value of the constant $k$

### 5.2 Revision Exercise

Any solution based entirely on graphical or numerical methods is not acceptable

Marks Available : 52

## Question 1

A-Level Examination Question, June 2018, Paper 1, Q6 (Edexcel)


The circle $C$ has centre $A$ with coordinates (7,5)
The line $l$, with equation $y=2 x+1$, is the tangent to $C$ at the point $P$ ( a ) Show that an equation of the line $P A$ is $2 y+x=17$
(b) Find an equation for $C$

The line with equation $y=2 x+k, k \neq 1$, is also a tangent to $C$
( c) Find the value of the constant $k$

## Question 2

Given that, $(7-\sqrt{3})(5-\sqrt{3})=a+b \sqrt{3}, \quad$ where $a$ and $b$ are integers,
find the value of $a$ and the value of $b$

## Question 3

(i) Complete the square for the following function,

$$
f(x)=x^{2}-8 x+23
$$

( ii ) Use your part (i) answer to explain why the graph of the function will not have any $x$-axis crossing points
(iii) Given your previous answers, would you expect the discriminant of the function to be positive, negative or zero?
[ 1 mark ]

## Question 4

Given that, $\frac{\sqrt{3}}{3+2 \sqrt{3}}=m+n \sqrt{3}$, where $m$ and $n$ are integers,
find the value of $m$ and the value of $n$

## Question 5

Given that,

$$
5 x^{2}+10 x-2=a(x+b)^{2}+c
$$

where $a, b$ and $c$ are integers, find the value of $a$, the value of $b$ and the value of $c$

## Question 6

Find the set of values of $x$ for which
(i) $3(2 x+1)>5-2 x$
(ii) $2 x^{2}-7 x+3>0$
(iii) both $3(2 x+1)>5-2 x$
and $2 x^{2}-7 x+3>0$

## Question 7

AS-Level Examination Question, June 2018, Q14 (Edexcel)
The circle $C$ has equation

$$
x^{2}+y^{2}-6 x+10 y+9=0
$$

(a) Find
(i) the coordinates of the centre of $C$
(ii) the radius of $C$

The line with equation $y=k x$, where $k$ is a constant, cuts $C$ at two distinct points
(b) Find the range of values of $k$

## Question 8

$$
f(x)=x^{2}+(k+3) x+k \text { where } k \text { is a real constant }
$$

( a ) Find the discriminant of $f(x)$ in terms of $k$
(b) Show that the discriminant of $f(x)$ can be expressed in the form $(k+a)^{2}+b$ where $a$ and $b$ are integers to be found.
(c) Show that, for all values of $k$, the equation $f(x)=0$ has real roots

## Question 9

Solve the equation, $8^{2 x}-10\left(8^{x}\right)+16=0$

## Question 10

$$
m(x)=x^{4}+2 x^{3}-3 x^{2}-8 x-4
$$

Factorise the quartic polynomial completely.

